



Eastern Mediterranean University

"For Your International Career"

Faculty of Engineering

ELECTRICAL AND ELECTRONIC ENGINEERING DEPARTMENT

EENG223 – Circuit Theory I

**Final Exam
Spring 2014-15**

**02 July 2015
Duration: 120 minutes**

Instructor: M. K. Uyguroğlu

| STUDENT'S | |
|-----------|-----------|
| NUMBER | |
| NAME | SOLUTIONS |
| SURNAME | |
| GROUP NO. | |

| Problem | | Points |
|---------|--|--------|
| 1 | | 20 |
| 2 | | 20 |
| 3 | | 20 |
| 4 | | 20 |
| 5 | | 20 |
| TOTAL | | 100 |

Problem 1

The mesh equations for the circuit shown in Fig.P1 are

$$\begin{bmatrix} 8 & -2 & -5 \\ -2 & 5 & -3 \\ -5 & -3 & 18 \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \\ i_3 \end{bmatrix} = \begin{bmatrix} 3 \\ 3 \\ 0 \end{bmatrix}$$

Given $V_3 = 5 \text{ V}$, find R_1, R_2, R_3, R_4, R_5 , and V_1, V_2 .

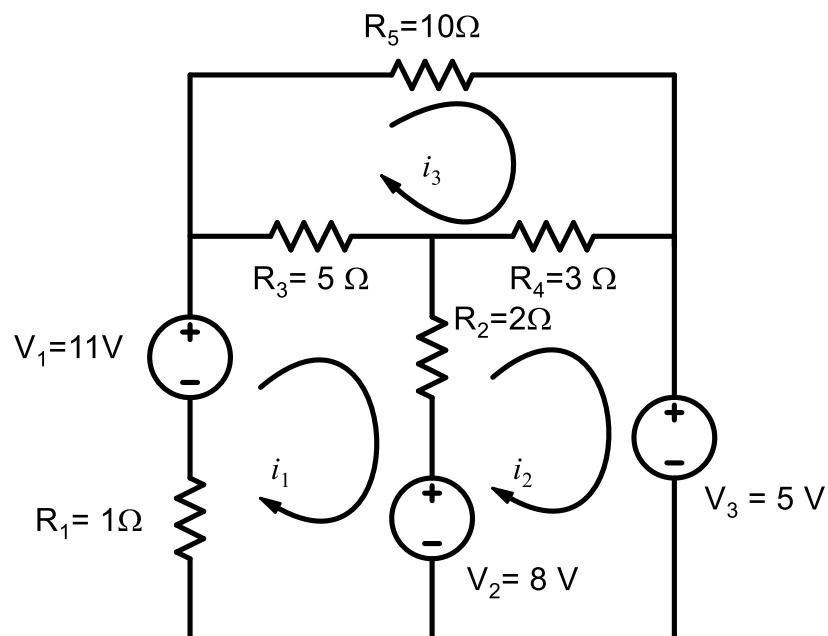


Figure P1

Problem 2

Using nodal analysis find i_x in the circuit shown in Fig.P2.

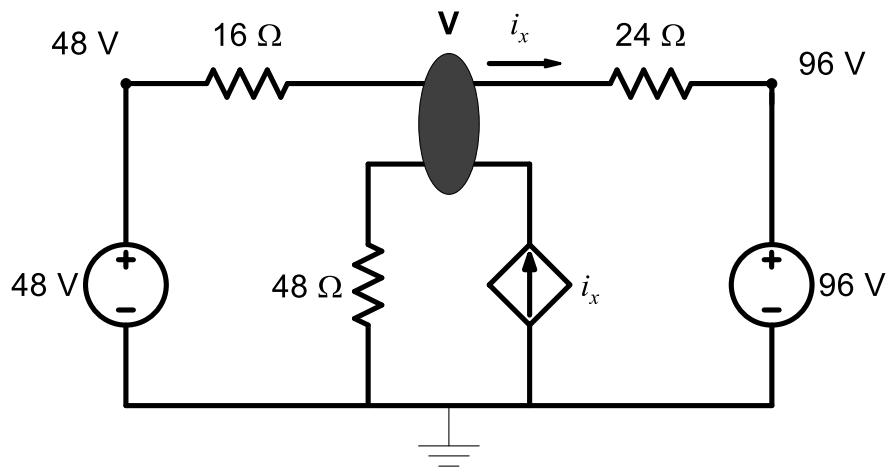


Figure P2

KCL at V:

$$\frac{V-48}{16} + \frac{V-96}{24} + \frac{V}{48} = i_x = \frac{V-96}{24}$$

$$\left(\frac{1}{16} + \frac{1}{48} \right) V = \frac{48}{16} = 3$$

Multiply both sides of the equation by 48 yields:

$$4V = 3(48) \Rightarrow V = 36 \text{ V}$$

Therefore

$$i_x = \frac{36-96}{24} = -\frac{60}{24} = -2.5 \text{ A}$$

Problem 3

Determine the current i_0 for the circuit shown in Fig.P3.

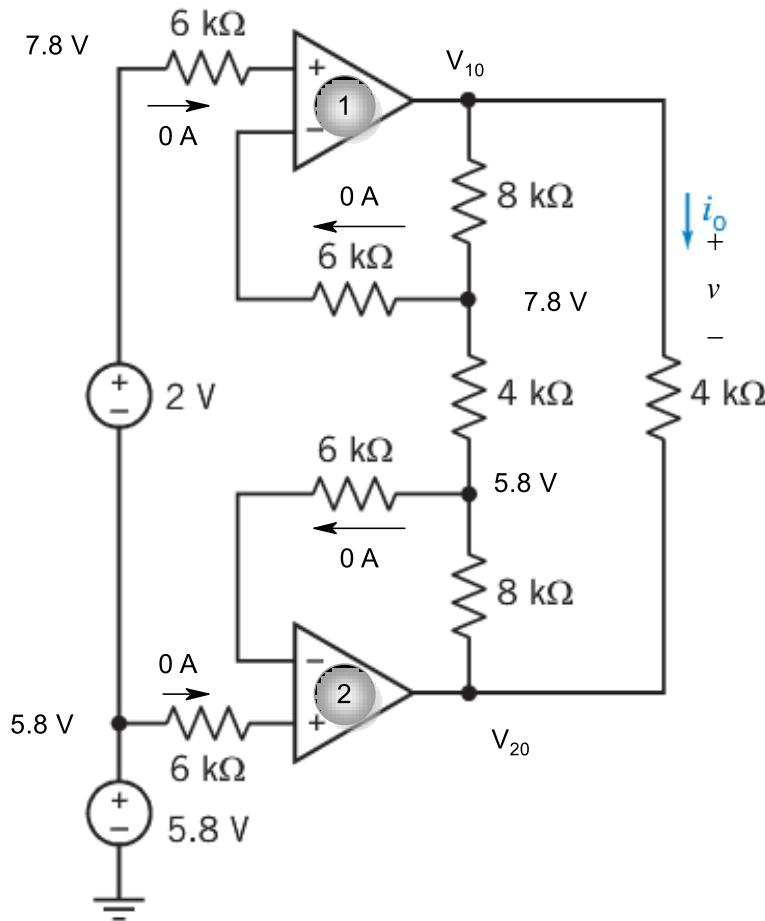


Figure P3

KCL at inverting terminal of OP AMP (1)

$$\frac{7.8 - 5.8}{4k} + \frac{7.8 - V_{10}}{8k} = 0$$

Multiply both sides by $8k$.

$$4 + 7.8 = V_{10} \Rightarrow V_{10} = 11.8\text{ V}$$

KCL at inverting terminal of OP AMP (2)

$$\frac{5.8 - 7.8}{4k} + \frac{5.8 - V_{20}}{8k} = 0$$

Multiply both sides by $8k$.

$$-4 + 5.8 = V_{20} \Rightarrow V_{20} = 1.8\text{ V}$$

$$i_0 = \frac{11.8 - 1.8}{4k} = 2.5mA$$

Problem 4

The circuit shown in Fig. P4 is under dc conditions before the switch closes at time $t = 0$. Determine $v(t)$ for $t > 0$.

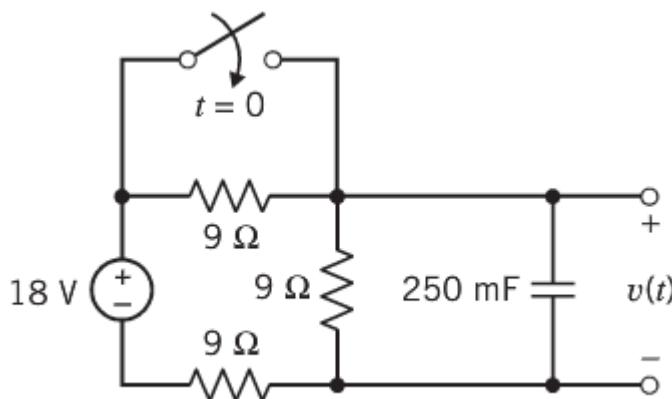
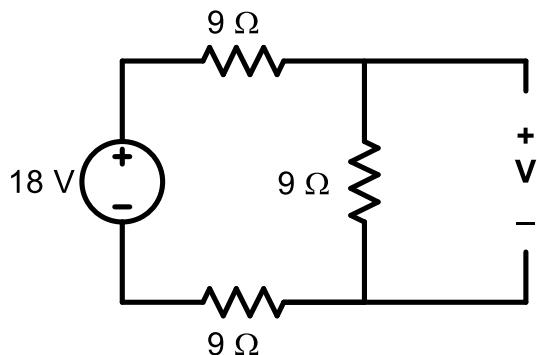


Figure P4

at $t = 0^-$

(since the circuit is under dc conditions, capacitor acts like open circuit)



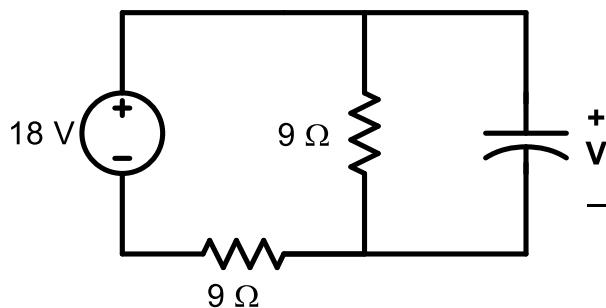
Using voltage division principle

$$V(0^-) = 18 \frac{9}{27} = 6 \text{ V}$$

Since the capacitor voltage cannot change instantaneously,

$$V(0^-) = V(0^+) = 6 \text{ V}$$

For $t > 0$



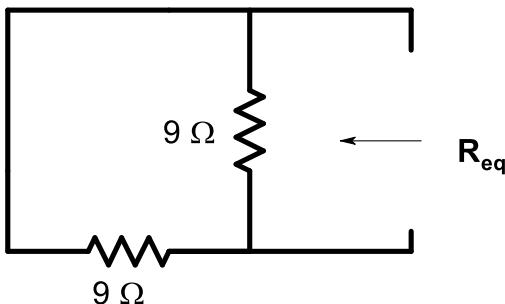
Since the circuit contains a dc source:

$$V(t) = V(\infty) + [V(0) - V(\infty)] e^{-\frac{t}{\tau}}$$

Where

$$\tau = R_{eq} C$$

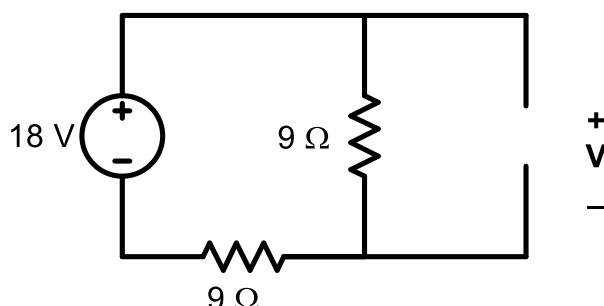
R_{eq} is the equivalent resistance seen by the capacitor by setting the independent source values to zero.



$$R_{eq} = 9 // 9 = 4.5 \Omega$$

$$\tau = 4.5 \times 250 \times 10^{-3} = \frac{4.5}{4} = 1.125 \text{ sec.}$$

At $t = \infty$, the circuit will be under dc conditions again.



Using voltage division principle

$$V(\infty) = 18 \frac{9}{18} = 9 \text{ V}$$

Therefore

$$V(t) = 9 + [6 - 9] e^{-0.89t}$$

$$V(t) = 9 - 3e^{-0.89t} \text{ V}$$

Problem 5

Suppose that the switch in Fig. P5 has been closed for a long time and is opened at $t = 0$. Find:

(a) $i(0+)$ and $v(0+)$

(b) $\frac{di(0+)}{dt}$

(c) $i(t)$ for $t > 0$

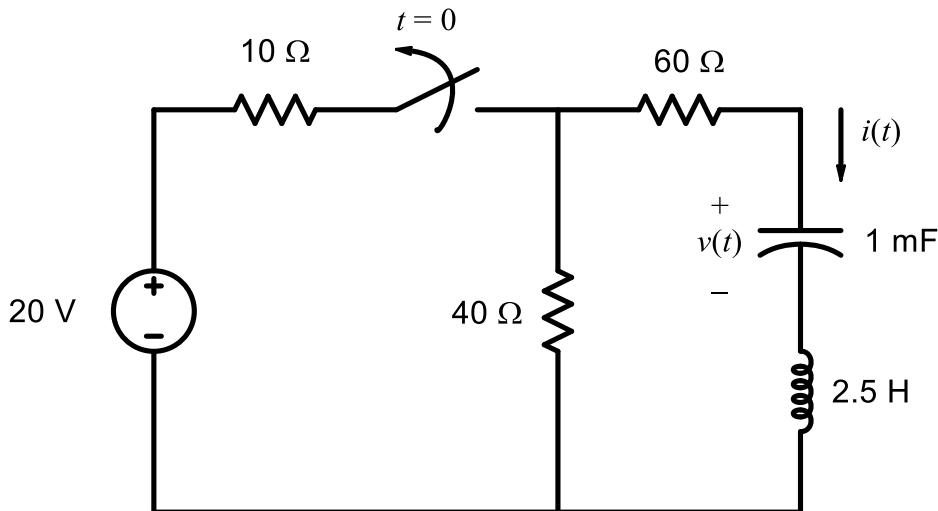
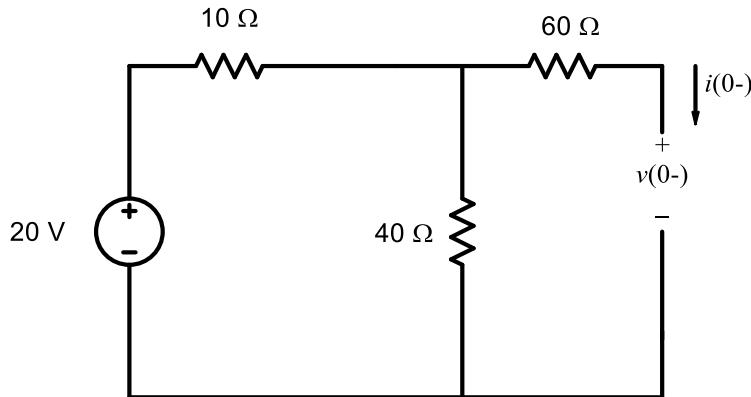


Figure P5

- (a) At $t = 0-$, the circuit is under dc conditions and inductor acts like short circuit and capacitor acts like open circuit.



It is obvious that

$i(0-) = 0$ and $v(0-)$ is the voltage across 40Ω resistor.

Therefore, using voltage division principle

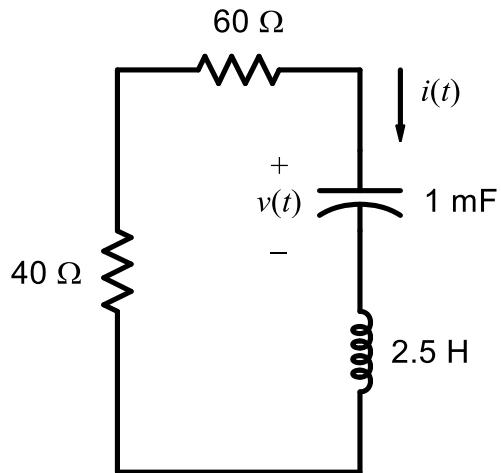
$$v(0-) = 20 \frac{40}{40+10} = 16 \text{ V}$$

Since the capacitor voltage and inductor current cannot change instantaneously,

$$v(0+) = v(0-) = 16 \text{ V}$$

$$i(0+) = i(0-) = 0$$

For $t > 0$



(b) If we write KVL around the loop:

$$2.5 \frac{di}{dt} + 40i + 60i + v = 0$$

$$2.5 \frac{di}{dt} + 100i + v = 0 \dots\dots\dots(1)$$

and

$$i = 1 \times 10^{-3} \frac{dv}{dt} \dots\dots\dots(2)$$

If we write Eqn.(1) at $t = 0+$

$$2.5 \frac{di(0+)}{dt} + 100i(0+) + v(0+) = 0$$

$$\frac{di(0+)}{dt} = -\frac{16}{2.5} = -6.4 \text{ A/s}$$

(c) From Eqn.(1):

$$v = -2.5 \frac{di}{dt} - 100i \dots\dots\dots(3)$$

Substitution of Eqn.(3) into (2) yields:

$$i = -2.5 \times 10^{-3} \frac{d^2i}{dt^2} - 100 \times 10^{-3} \frac{di}{dt}$$

If we multiply both sides of the equation by 400 and rearrange it, we can obtain:

$$\frac{d^2i}{dt^2} + 40 \frac{di}{dt} + 400i = 0$$

Characteristic equation is

$$s^2 + 40s + 400 = 0$$

$$(s + 20)(s + 20) = 0$$

Which implies that

$s_{1,2} = -20$ real and equal natural frequencies. (Critically damped case)

$$i(t) = e^{-20t} (A_1 + A_2 t)$$

$$i(0) = 0 = A_1$$

$$\frac{di}{dt} = -20e^{-20t} (A_1 + A_2 t) + A_2 e^{-20t}$$

$$\frac{di(0)}{dt} = -6.4 = -20A_1 + A_2$$

$$A_2 = -6.4$$

$$i(t) = -6.4te^{-20t} A$$