

HOMEWORK I DUE: Group1, 5 April 2017 and Group2, 6 April 2017

1. Express $(1965)_{10}$, $(367)_{10}$, $(29)_{10}$, in

- i. BCD
- ii. Excess-3
- iii. 2421

Decimal	1	9	6	5
BCD	0001	1001	0110	0101
Excess-3	0011	1100	1001	1000
2421	0001	1111	1100	1011

Decimal	3	6	7
BCD	0011	0110	0111
Excess-3	0110	1001	1010
2421	0011	1100	1101

Decimal	2	9
BCD	0010	1001
Excess-3	0101	1100
2421	0010	1111

2. Convert the following decimal numbers 77 and 38 to binary using the signed 2's complement representation and enough digits to accommodate numbers. Then perform the binary equivalent of $(+77) + (-38)$, $(-77) + (+38)$ and $(-77) + (-38)$.

77	2 = 38	1	38	2 = 19	0
38	2 = 19	0	19	2 = 9	1
19	2 = 9	1	9	2 = 4	1
9	2 = 4	1	4	2 = 2	0
4	2 = 2	0	2	2 = 1	0
2	2 = 1	0	1	2 = 0	1
1	2 = 0	1			
77 = (1001101) ₂			38 = (100110) ₂		

Therefore for sign 2's complement representation of

+77	01001101	-77	10110011
+38	00100110	-38	11011010

(+ 77)	01001101
+ (- 38)	+ 11011010
(+39)	10010011 most significant bit is discarded.

(- 77)	10110011
+ (+ 38)	+ 00100110
(- 39)	11011001 signed 2's complement of -39.

(- 77)	10110011
+ (- 38)	+ 11011010
(- 115)	110001101 most significant bit is discarded. The rest is signed 2's complement of -115.

3. The following is a string of ASCII characters whose bit patterns have been converted into hexadecimal for compactness: 23 CE EF F2 F4 C8 43 79 D0 F2 75 D3. Of the 8 bits in each pair of digits, the leftmost is a parity bit. The remaining bits are the ASCII code.

i. Convert to bit form and decode the ASCII.

Hex	Parity	ASCII		Hex	Parity	ASCII	
23	0	010 0011	#	43	0	100 0011	C
CE	1	100 1110	N	79	0	111 1001	y
EF	1	110 1111	o	D0	1	101 0000	P
F2	1	111 0010	r	F2	1	111 0010	r
F4	1	111 0100	t	75	0	111 0101	u
C8	1	100 1000	H	D3	1	101 0011	S

ii. Determine the parity used: odd or even.

Odd

4. Without simplification for a given Boolean function $x' + xy + xz (y' + z) + (xz)'$.

i. Find the dual of the expression.

$$= x' (x+y) (x+z) + (y'z) (x+z)'$$

ii. Find the complement of the expression.

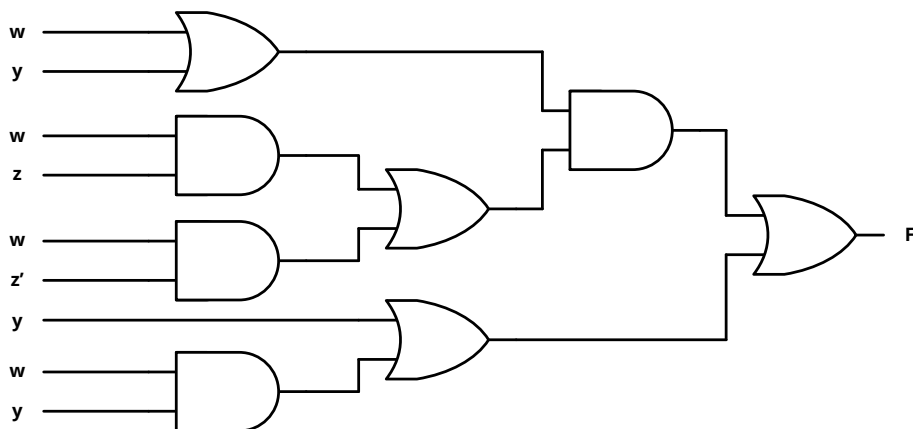
$$= x (x'+y') (x'+z') + (yz') (x'+z)$$

5. Given the Boolean function $F = (w+y)(wz + wz') + wy + y$

i. Obtain the truth table of the function.

w	x	y	z	z'	w+y	wz	wz'	wz+wz'	(w+y)(wz+wz')	wy	wy+y	F
0	0	0	0	1	0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0	0	0	0	0	0
0	0	1	0	1	1	0	0	0	0	0	1	1
0	0	1	1	0	1	0	0	0	0	0	1	1
0	1	0	0	1	0	0	0	0	0	0	0	0
0	1	0	1	0	0	0	0	0	0	0	0	0
0	1	1	0	1	1	0	0	0	0	0	1	1
0	1	1	1	0	1	0	0	0	0	0	1	1
1	0	0	0	1	1	0	1	1	1	0	0	1
1	0	0	1	0	1	1	0	1	1	0	0	1
1	0	1	0	1	1	0	1	1	1	1	1	1
1	0	1	1	0	1	1	0	1	1	1	1	1
1	1	0	0	1	1	0	1	1	1	0	0	1
1	1	0	1	0	1	1	0	1	1	0	0	1
1	1	1	0	1	1	0	1	1	1	1	1	1
1	1	1	1	0	1	1	0	1	1	1	1	1

ii. Draw the logic diagram using the Boolean expression.



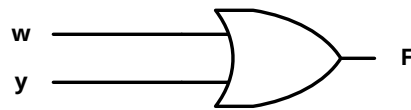
- iii. Simplify the function to a minimum number of literals using Boolean algebra.

$$\begin{aligned}
 F &= (w+y) (wz + wz') + wy + y \\
 &= (w + y) w(z+z') + wy + y \\
 &= (w + y) w (1) + wy + y \\
 &= (w + y) w + wy + y \\
 &= (w.w + wy) + wy + y \\
 &= w + wy + wy + y \\
 &= w + wy + 1 \\
 &= w (1+y) + y \\
 &= w (1) + y \\
 &= w + y
 \end{aligned}$$

- iv. Obtain the truth table of the function from the simplified expression and show that it is the same as the one in part (i).

w	x	y	z	w+y	=	F (i)
0	0	0	0	0		0
0	0	0	1	0		0
0	0	1	0	1		1
0	0	1	1	1		1
0	1	0	0	0		0
0	1	0	1	0		0
0	1	1	0	1		1
0	1	1	1	1		1
1	0	0	0	1		1
1	0	0	1	1		1
1	0	1	0	1		1
1	0	1	1	1		1
1	1	0	0	1		1
1	1	0	1	1		1
1	1	1	0	1		1
1	1	1	1	1		1

- v. Draw the logic diagram from the simplified expression and compare the total number of gates with the diagram of part (ii).



6. Express the following function in sum of products and product of sums.

$$F(A,B,C,D) = ABD' + AB + BC' + C'D'$$

STEP1:

$$ABD' (C + C') = \mathbf{ABCD'} + \mathbf{ABC'D'}$$

STEP2:

$$AB (C + C') = ABC + ABC'$$

$$ABC (D + D') + ABC' (D + D') = \mathbf{ABCD} + \mathbf{ABCD'} + \mathbf{ABC'D} + \mathbf{ABC'D'}$$

STEP3:

$$BC' (A + A') = ABC' + A'BC'$$

$$ABC' (D + D') + A'BC' (D + D') = \mathbf{ABC'D} + \mathbf{ABC'D'} + \mathbf{A'BC'D} + \mathbf{A'BC'D'}$$

STEP4:

$$C'D' (A + A') = AC'D' + A'C'D'$$

$$AC'D' (B + B') + A'C'D' (B + B') = \mathbf{ABC'D'} + \mathbf{AB'C'D'} + \mathbf{A'BC'D'} + \mathbf{A'B'C'D'}$$

$F = \mathbf{ABCD'} + \mathbf{ABC'D'} + \mathbf{ABCD} + \mathbf{ABC'D} + \mathbf{A'BC'D} + \mathbf{A'BC'D'} + \mathbf{ABC'D'} + \mathbf{A'B'C'D'}$								
F =	1110	1100	1111	1101	0101	0100	1000	0000
F =	m14	m12	m15	m13	m5	m4	m8	m0
$F(A,B,C,D) = \sum (0,4,5,8,12,13,14,15)$								
$F(A,B,C,D) = \prod (1,2,3,6,7,9,10,11)$								

7. Simplify the following Boolean function using K-Map by first finding the essential prime implicants.

$$F(w,x,y,z) = \Sigma(0,2,4,5,6,7,8,10,13,15)$$

		yz			
wx		00	01	11	10
00		1	0	0	1
01		1	1	1	1
11			1	1	
10		1			1

Essential Prime Implicants: $F = x'z' + xz$

Prime Implicants: $F = w'x$

So $F = x'z' + xz + w'x$

8. Simplify the following Boolean function F, together with the don't care conditions d and then express the simplified function in sum of minterms and product of maxterms.

$$F(A,B,C,D) = \Sigma(1,3,5,7,9,15),$$

$$d(A,B,C,D) = \Sigma(4,6,12,13)$$

		CD			
AB		00	01	11	10
00		0	1	1	0
01		X	1	1	X
11		X	X	1	0
10		0	1	0	0

$$F = C'D + A'D + BD \text{ (SOP)}$$

$$F' = B'D' + BD' + AB'C$$

$$F = (B + D)(B' + D) + (A' + B + C')$$