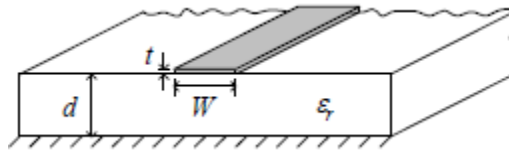


PLANAR TRANSMISSION LINES

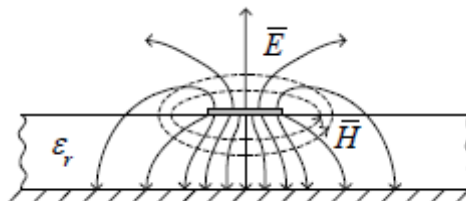
Definition: A planar TL is a TL with conducting metal strips that lie entirely in parallel planes. The most common structure is one or more parallel metal strips placed on a dielectric substrate material adjacent to a conducting ground plane. A planar TL that is widely used is the microstrip line.



It consists of a single conducting strip of width W placed on a dielectric substrate of thickness d and located on a ground plane.

MICROSTRIP TRANSMISSION LINE

In a microstrip TL the dielectric material does not completely surround the metallic strip and hence the fundamental mode of propagation is not a pure TEM mode. At low frequencies, typically a few gigahertz, for practical microstrip lines, E_z and H_z have far smaller amplitudes than the corresponding transverse components. So, the mode is a quasi-TEM mode.



In most practical applications, the dielectric substrate is electrically very thin ($d \ll \lambda$), and so the fields are quasi-TEM. In other words, the fields are essentially the same as those of the static case.

Quasi – TEM Approximation (Low frequency approximation)

1) Pozar's Approximation

The phase velocity and the propagation constant can be expressed as:

$$v_p = \frac{c}{\sqrt{\epsilon_e}}, \quad \beta = k_0 \sqrt{\epsilon_e} \text{ where}$$

ϵ_e = effective dielectric constant of the microstrip line and

$$1 < \epsilon_e < \epsilon_r$$

$$\epsilon_e = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \cdot \frac{1}{\sqrt{1 + 12 \frac{d}{w}}}$$

The characteristic impedance:

$$Z_0 = \left\{ \begin{array}{l} \frac{60}{\sqrt{\epsilon_e}} \ln \left(\frac{8d}{w} + \frac{w}{4d} \right) \quad \text{for } \frac{w}{d} \leq 1 \\ \frac{120\pi}{\sqrt{\epsilon_e} \left[\frac{w}{d} + 1.393 + 0.667 \ln \left(\frac{w}{d} + 1.444 \right) \right]} \quad \text{for } \frac{w}{d} \geq 1 \end{array} \right\}$$

For a given Z_0 and ϵ_r , the $\frac{w}{d}$ ratio can be found from:

$$\frac{w}{d} = \begin{cases} \frac{8e^A}{e^{2A} - 2}, & \text{for } \frac{w}{d} < 2 \\ \frac{2}{\pi} \left[B - 1 - \ln(2B - 1) + \frac{\epsilon_r - 1}{2\epsilon_r} \left\{ \ln(B - 1) + 0.39 - \frac{0.61}{\epsilon_r} \right\} \right], & \text{for } \frac{w}{d} > 2 \end{cases}$$

Where

$$A = \frac{Z_0}{60} \sqrt{\frac{\epsilon_r + 1}{2}} + \frac{\epsilon_r - 1}{\epsilon_r + 1} \left(0.23 + \frac{0.11}{\epsilon_r} \right)$$

$$B = \frac{377\pi}{2Z_0\sqrt{\epsilon_r}}$$

The attenuation can be calculated from:

$$\alpha_d = \frac{k_0 \epsilon_r (\epsilon_e - 1)}{2\sqrt{\epsilon_e} (\epsilon_r - 1)} \tan \delta \quad (Np / m)$$

$$\alpha_c = \frac{R_s}{Z_0 w} \quad (Np / m)$$

2) Collin's Approximation

$$\epsilon_e = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \left(1 + \frac{12d}{w} \right)^{-1/2} + F(\epsilon_r, d) - 0.217(\epsilon_r - 1) \frac{t}{\sqrt{wd}}$$

Where

$$F(\epsilon_r, d) = \begin{cases} 0.02(\epsilon_r - 1) \left(1 - \frac{w}{d}\right)^2 & \text{for } \frac{w}{d} < 1 \\ 0 & \text{for } \frac{w}{d} > 1 \end{cases}$$

$$Z_0 = \left(\frac{\epsilon_0 \mu_0}{\epsilon_e} \right)^{1/2} \frac{1}{C_a}$$

$$C_a = \begin{cases} \frac{2\pi\epsilon_0}{\ln\left(\frac{8d}{w} + \frac{w}{4d}\right)}, & \frac{w}{d} \leq 1 \\ \epsilon_0 \left[\frac{w}{d} + 1.393 + 0.667 \ln\left(\frac{w}{d} 1.444\right) \right] & \frac{w}{d} > 1 \end{cases}$$

Example:

A microstrip line uses a substrate with $\epsilon_r = 9.7$ (alumina) and $d = 0.5\text{mm}$. The strip width is $w = 0.5\text{mm}$. Find ϵ_e , Z_0 and the microstrip wavelength at $f = 2\text{GHz}$.

Solution:

Pozar:

$$\epsilon_e = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \cdot \frac{1}{\sqrt{1 + 12 \frac{d}{w}}}$$

$$\varepsilon_e = \frac{9.7+1}{2} + \frac{9.7-1}{2} \cdot \frac{1}{\sqrt{1+12}} = 6.556$$

$$Z_0 = \frac{60}{\sqrt{\varepsilon_e}} \ln\left(\frac{8d}{w} + \frac{w}{4d}\right)$$

$$Z_0 = \frac{60}{\sqrt{6.556}} \ln\left(8 + \frac{1}{4}\right) = 49.449\Omega$$

$$\lambda = \frac{2\pi}{\beta} = \frac{2\pi}{k_0\sqrt{\varepsilon_e}} = \frac{\lambda_0}{\sqrt{\varepsilon_e}}$$

$$\lambda_0 = \frac{c}{f} = \frac{3 \times 10^8}{2 \times 10^9} = 15 \text{ cm}$$

$$\lambda = \frac{\lambda_0}{\sqrt{\varepsilon_e}} = \frac{15}{\sqrt{6.556}} = 5.858 \text{ cm}$$

Collin

Since $F(\varepsilon_r, d) = 0$, we have the same results.

Example:

Consider the microstrip line in the above example. Assume $\tan \delta = 2 \times 10^{-4}$ and $t = 0.02 \text{ mm}$. If $f = 4 \text{ GHz}$, calculate the total attenuation (assume copper).

Solution:

$$\epsilon_e = 6.556, Z_0 = 49.449 \Omega, \lambda_0 = 7.5 \text{ cm}$$

$$\alpha_d = \frac{\pi}{\lambda_0} \frac{\epsilon_r}{\sqrt{\epsilon_e}} \left(\frac{\epsilon_e - 1}{\epsilon_r - 1} \right) \tan \delta = \frac{\pi}{7.5} \frac{9.7}{\sqrt{6.556}} \left(\frac{6.556 - 1}{9.7 - 1} \right) 2 \times 10^{-4}$$

$$\alpha_d = 2.02 \times 10^{-4} (\text{Np} / \text{cm})$$

$$\alpha_c = \frac{R_s}{Z_0 w}$$

$$R_s = \sqrt{\frac{\omega \mu}{2 \sigma}} = \sqrt{\frac{\pi f \mu_0}{\sigma}} = \sqrt{\frac{\pi \times 4 \times 10^9 \times 4 \pi \times 10^{-7}}{5.7 \times 10^7}} = 16.64 \times 10^{-3} \Omega$$

$$\alpha_c = \frac{16.64 \times 10^{-3}}{49.449 \times 0.5 \times 10^{-3}} = 0.673 \text{ Np} / \text{m} = 67.3 \times 10^{-4} (\text{Np} / \text{cm})$$

$$\alpha = \alpha_c + \alpha_d = 69.32 \times 10^{-4} (\text{Np} / \text{cm})$$