

**EENG/INFE 226 SIGNALS AND SYSTEMS**  
**LAB 4**  
**THE CONVOLUTION SUM & INTEGRAL**

1) a) Consider The Finite-length Signal

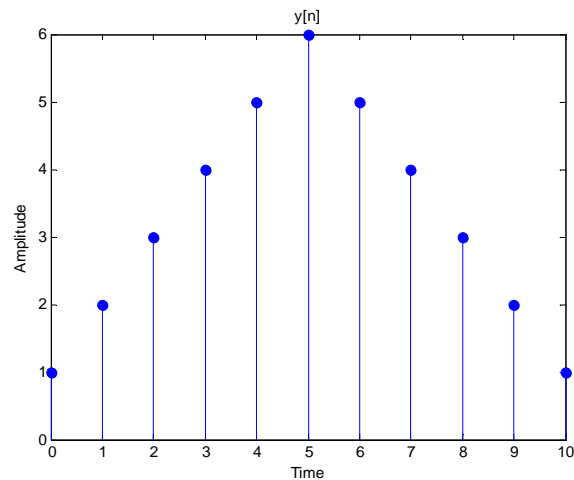
$$x[n] = \begin{cases} 1 & 0 \leq n \leq 5 \\ 0 & \text{otherwise} \end{cases}$$

Analytically determine  $y[n]=x[n]*x[n]$

b) Compute the nonzero samples of  $y[n]=x[n]*x[n]$  using *conv*, and store these samples in the vector *y*. Your first step should be define the vector *x* to contain the samples of  $x[n]$  on the interval  $0 \leq n \leq 5$ . Also construct an index vector *ny*, where  $ny(i) = y[ny(i)]$ . For example,  $ny(1)$  should contain  $nx+nx$ , where  $nx$  is the first nonzero index of  $x[n]$ . Plot your results using *stem(ny,y)* and make sure that your plot agrees with the signal determined in part i.

**Answer:**

```
n=[0:5];
x=ones(1,length(n));
y=conv(x,x);
ny=[0:10];
figure(1)
stem(ny,y,'filled')
xlabel('Time')
ylabel('Amplitude')
title('y[n]')
```



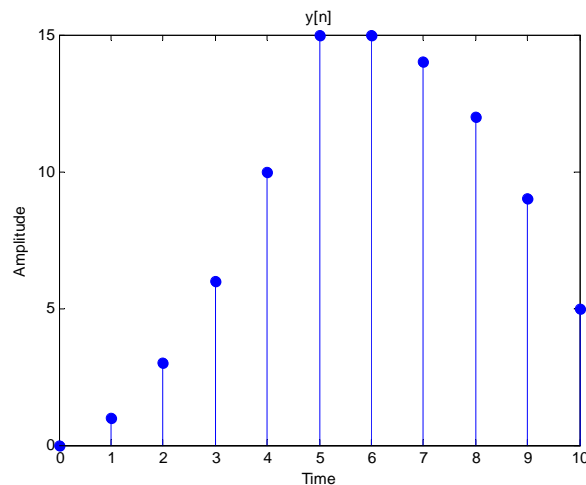
2) i) Consider the finite-length signal

$$x[n] = \begin{cases} n & 0 \leq n \leq 5 \\ 0 & \text{otherwise} \end{cases}$$

Analytically compute  $y[n]=x[n]*h[n]$ . Next, compute *y* using *conv*, where your first step should be to define the vector *h* to contain  $h[n] = u[n]$  on the interval  $0 \leq n \leq 5$ . Again construct a vector *ny* which contains the interval of *n* for which *y* contains  $y[n]$ . Plot your results *stem(ny,y)*.

**Answer:**

```
n=[0:5];
h=ones(1,length(n));
x=[0:5]; % x=n;
y=conv(x,h);
ny=[0:10];
figure(1)
stem(ny,y,'filled')
xlabel('Time')
ylabel('Amplitude')
title('y[n]')
```

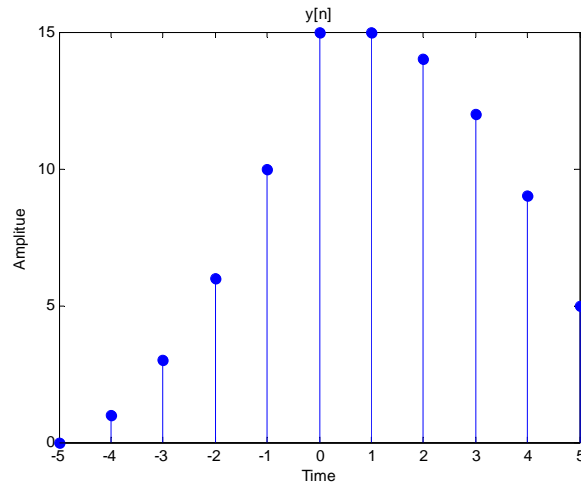


ii) How does  $y_2[n]=x[n]*h[n+5]$  compare to the signal  $y[n]$  derived in part i ?

iii) Use conv to compute the nonzero samples of  $y_2[n]$ , and store these samples in the vector  $y_2$ . If done correctly, this vector should be identical to the vector  $y$  computed in part ii. The only difference is that the indices, and store them in the vector  $ny_2$ . Plot  $y_2[n]$  using `stem(ny2,y2)`

### Answer:

```
ny=[-5:5];
h=[1 1 1 1 1 1];
x=[0 1 2 3 4 5 ];
y2=conv(x,h);
figure(1)
stem(ny,y2, 'filled')
xlabel('Time')
ylabel('Amplitude')
title('y[n]')
```

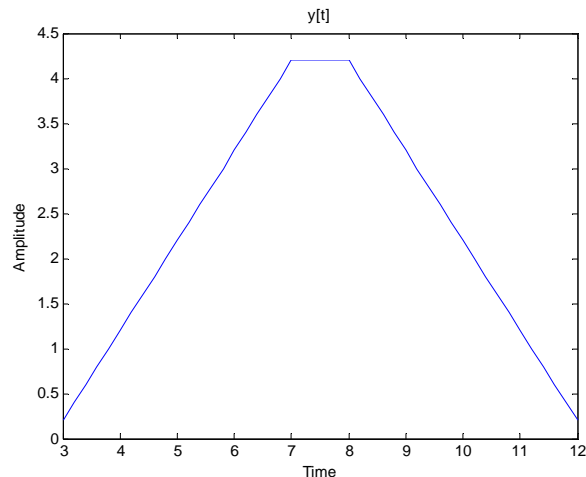


$$3) x(t) = \begin{cases} 1 & 1 \leq t \leq 5 \\ 0 & \text{otherwise} \end{cases} \quad h(t) = \begin{cases} 1 & 2 \leq t \leq 7 \\ 0 & \text{otherwise} \end{cases}$$

Using the MATLAB, generate these two functions and find the convolution of  $x(t)$  and  $h(t)$

### Answer:

```
Ts=0.2;
t1=[1:Ts:5];
t2=[2:Ts:7];
t3=[3:Ts:12];
x=ones(1,length(t1));
h=ones(1,length(t2));
y=Ts*conv(x,h);
figure(1)
plot(t3,y)
xlabel('Time')
ylabel('Amplitude')
title('y[t]')
```



### Home work:

Use matlab to generate the following two functions and find the convolution of them:

a)  $x(t)=\cos(\pi t/2)[u(t)-u(t-10)]$  ,  $h(t)=\sin(\pi t)[u(t-3)-u(t-12)]$ .

b)  $x[n]=3n$  for  $-1 < n < 6$  ,  $h[n]=1$  for  $4 < n < 13$ .

Print and submit the full program with the graphs on papers next lab session.