

EENG/INFE 226 SIGNALS AND SYSTEMS

LAB 6

FOURIER SERIES and FOURIER TRANSFORM REPRESENTATION

Objective

The objective of this experiment is to introduce using MATLAB to perform Discrete-Time Fourier Series (DTFS), Continuous-Time Fourier Series (CTFS), and to compute the frequency response of a causal LTI-system.

6.1 Compute the DTFS with fft:

The discrete-time Fourier series (DTFS) is a frequency-domain representation for periodic discrete-time sequences. For a signal $x[n]$ with fundamental period N , the DTFS synthesis and analysis equations are given by:

$$x[n] = \sum_{k=0}^{N-1} X[k] e^{jk(2\pi/N)n} \dots\dots\dots \text{synthesis}$$

$$X[k] = \frac{1}{N} \sum_{n=0}^{N-1} x[n] e^{-jk(2\pi/N)n} \dots\dots\dots \text{analysis}$$

x : represent one period of an N periodic signal.
 X : gives DTFS coefficient as a vector.

MATLAB contains two very efficient routines for computing Analysis and synthesis:

- If x is an N -point vector containing $x[n]$ for the period $0 \leq n \leq N-1$, then the DTFS of $x[n]$ can be computed by:

$$\gg X = (1/N) * fft(x).$$

- If X is an N -point vector containing $X[k]$ for the period $0 \leq k \leq N-1$, then the synthesis of DTFS of $X[k]$ can be computed by:

$$\gg x = (N) * ifft(x).$$

Exercise 1:

Consider using MATLAB to solve Problem 3.3(a) in (Simon Haykin 2nd Edition) book. For the DTFS coefficient, the signal:

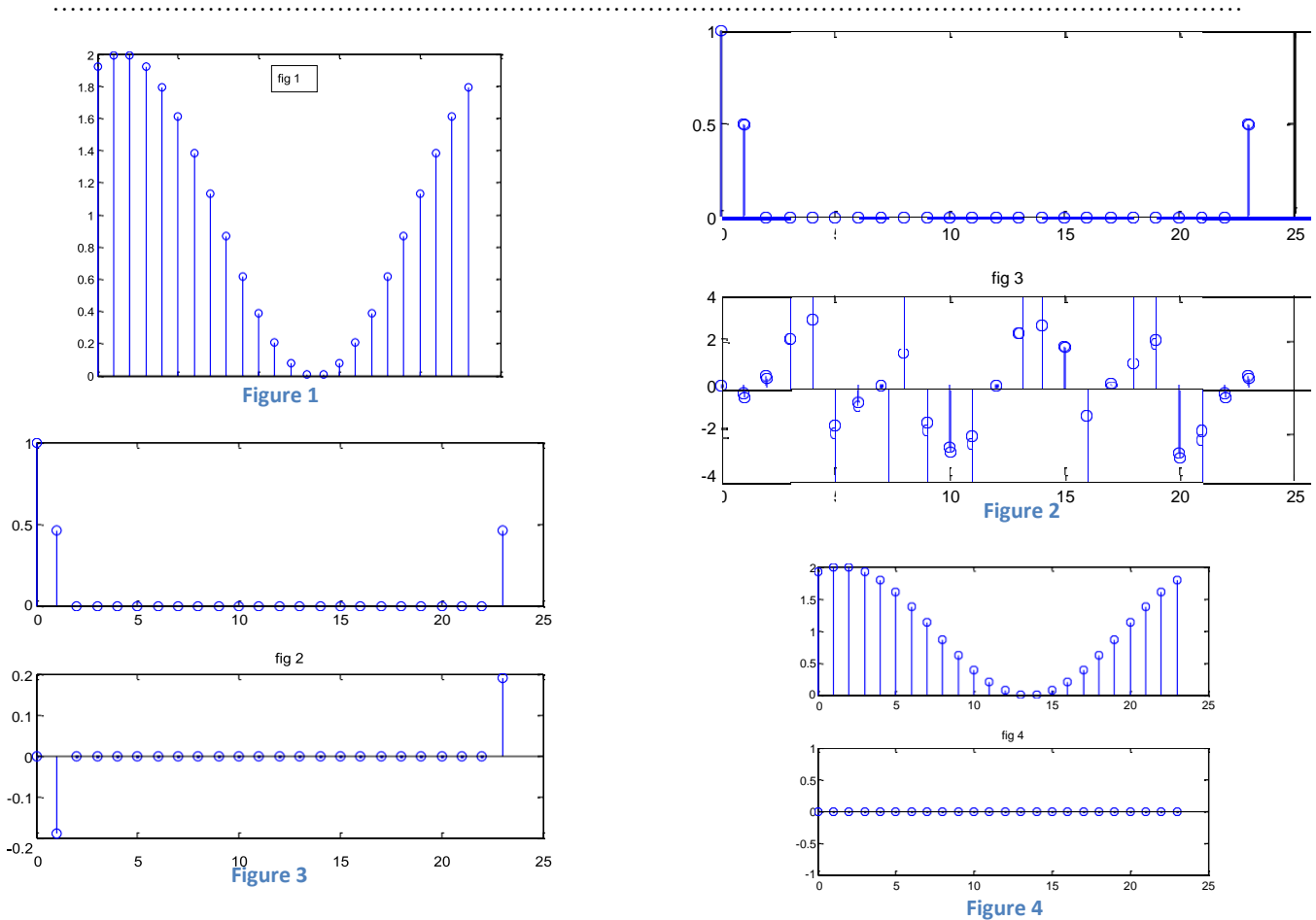
$$x[n] = 1 + \sin\left(\frac{n\pi}{12} + \frac{3\pi}{8}\right)$$

This signal has period $N=24$.

Procedure:

- Define the signal period N .
- Define the index vector n to range from 0 to 23.
- Define the signal x as a vector of ones using the (**ones**) command plus sin value. Also plot the signal in figure 1 using **stem**.
- Use the function (**fft**) function to evaluate the DTFS coefficients. and store it in X .
- Plot the *real* and *imaginary* parts of fourier series coefficient x using **subplot** and **stem** on figure 2.
- Plot the *absolute value* and *angles* of fourier series coefficient x using **subplot** and **stem** on figure 3.
- Use the function (**ifft**) function to reconstruct the original time domain signal x . and store it in x_{recon} . Plot it on figure 4 as *real* and *imaginary* part using subplot.

Q: Comment on the relationship between figures of $x[n]$ and x_{recon} ?



6.1 Frequency Response Of LTI System From Impulse Response:

For a causal LTI system described by a difference equation,

- the command `[H omega]=freqz (b,a,N)` computes the frequency response $H(e^{j\omega})$ at N evenly spaced frequencies between 0 and π , i.e., $\omega_k = (\pi/N)k$ for $0 \leq k \leq N-1$.
- the command `[H omega]=freqz (b,a,N,'whole')` computes the frequency response $H(e^{j\omega})$ at N evenly spaced frequencies between 0 and 2π , i.e., $\omega_k = (2\pi/N)k$ for $0 \leq k \leq N-1$.
- the coefficient vectors \underline{a} and \underline{b} specify the difference equation using the same format in lab 5.
- *freqz* returns $H(e^{j\omega})$ in \mathbf{H} and the frequencies ω_k in \mathbf{omega} .

Assignment:

Consider the following difference equation:

$$y[n] - 0.75y[n - 1] + 0.6y[n - 2] = 2x[n] - x[n - 2]$$

1) Evaluate the Frequency Response at 4 evenly spaced between 0 and π ?

Procedure:

- Define $\underline{\mathbf{a}}$ and $\underline{\mathbf{b}}$ to describe the previous causal LTI system as a vectors.
- Use *freqz* with the coefficients $\underline{\mathbf{a}}$ and $\underline{\mathbf{b}}$ define \mathbf{HI} to be the value of the frequency response at 4 evenly spaced frequencies between 0 and π and $\mathbf{omega1}$ to be those frequencies.

2) Evaluate the Frequency Response at 4 evenly spaced between 0 and 2π ?